

**University of Stuttgart**  
Germany

# Clustering for Stacked Edge Splatting

Moataz Abdelaal<sup>1</sup>, Marcel Hlawatsch<sup>1</sup>, Michael Burch<sup>2</sup>, Daniel Weiskopf<sup>1</sup>

<sup>1</sup>University of Stuttgart, Germany

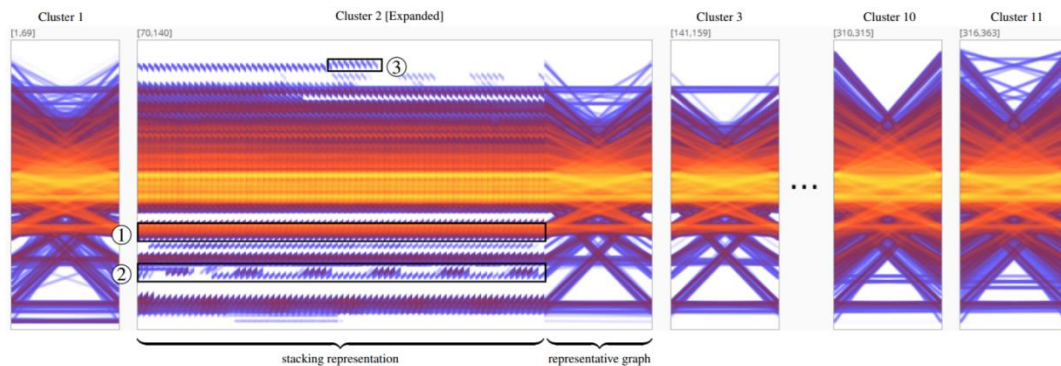
<sup>2</sup>TU Eindhoven, Netherlands

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Joint Conference GCPR/VMV 2018 | University of Stuttgart, Stuttgart, Germany |  
October 10-12, 2018

# Overview

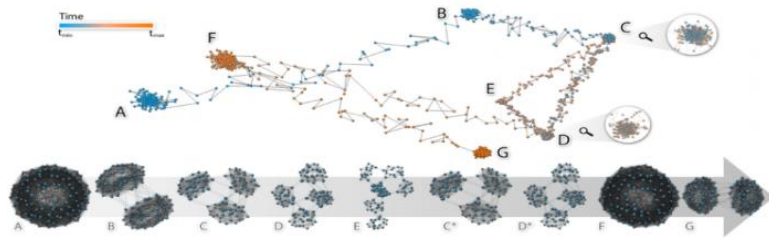
- Dynamic graph data
- Time-scalable overview
  - Temporal patterns
  - Temporal phases
  - Structural information



A dynamic graph visualization depicting the US domestic flight dataset

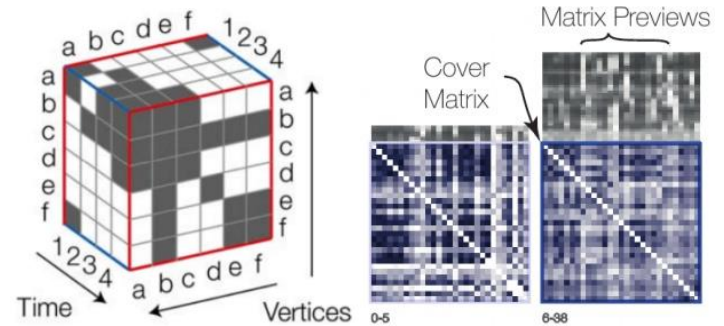
# Related Work

- Reducing graphs to points
- Graphs are considered points in high-dimensional space
- Scalability concerns w.r.t. graph size and number of time steps
- Harder to interpret the resulting dimensions



Reducing Snapshots to Points  
Van den Elzen et al. [vdEHBvW16]

- Adjacency matrices
- Cubix
- Small MultiPiles
- Hard to use [GFC05] in long and dense dynamic graphs.



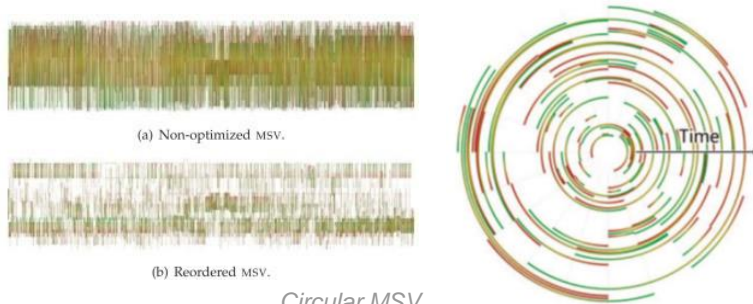
Cubix  
Bach et al. [BPF14]

MultiPiles  
Bach et al. [BHRD\*15]

[GFC05] GHONIEM M., FEKETE J., CASTAGLIOLA P.: On the readability of graphs using node-link and matrix-based representations: a controlled experiment and statistical analysis. *Information Visualization* 4, 2 (2005), 114–135. 2

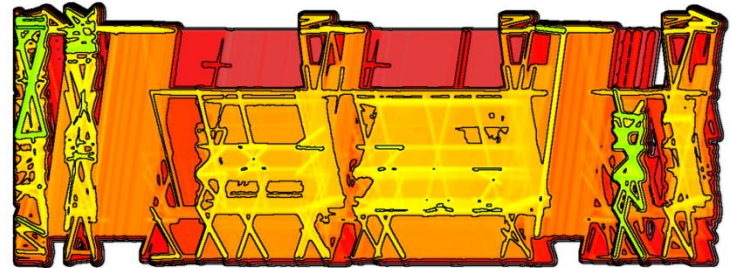
# Related Work

- Extended Massive Sequence View (MSV)
- Support different clustering and reordering techniques
- Circular MSV needs much screen space & introduces bias
- Temporal clustering not supported



*Circular MSV*  
Van den Elzen et al. [vdEHBvW13]

- Visualizing a Sequence of a Thousand Graphs
  - Pushing the individual graphs together by an interleaving them
  - Time-scalable but suffers from over-drawing problems



*Visualizing a Sequence of a Thousand Graphs*  
Burch et al. [BHW17]

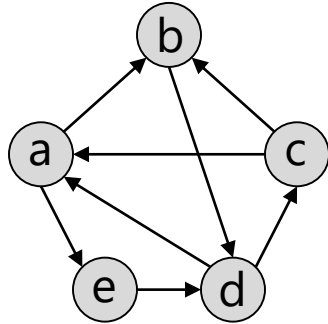
# Contributions

- 1) Introducing the *stacked edge splatting* representation
  - To avoid the over-drawing problems of the interleaving method -> uncover temporal patterns
  
- 2) Applying sequential temporal clustering
  - To identify temporal phases

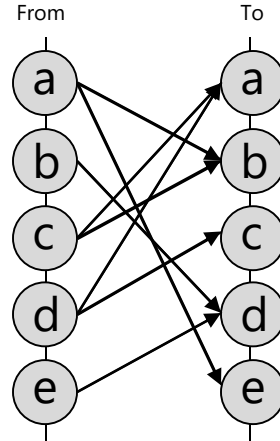
# Visualization Technique

Time	From	To	Weight
1	a	b	5
1	b	d	2
1	d	c	3
1	c	b	4
1	d	a	4
1	c	a	2
1	a	e	6
1	e	d	1
2	...	...	...

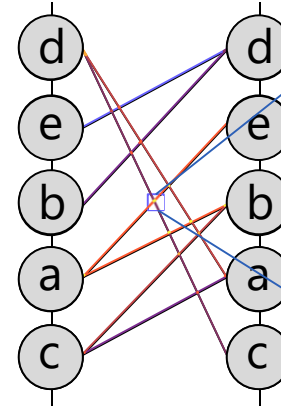
(a) Dataset



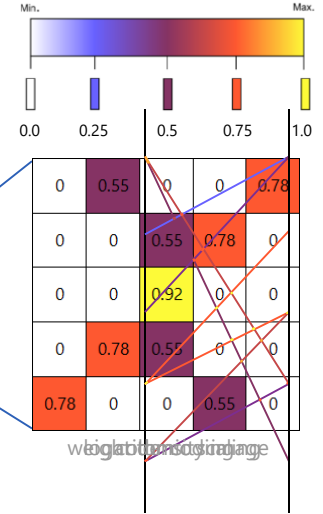
(b) Node-link diagram



(c) Bipartite graph layout

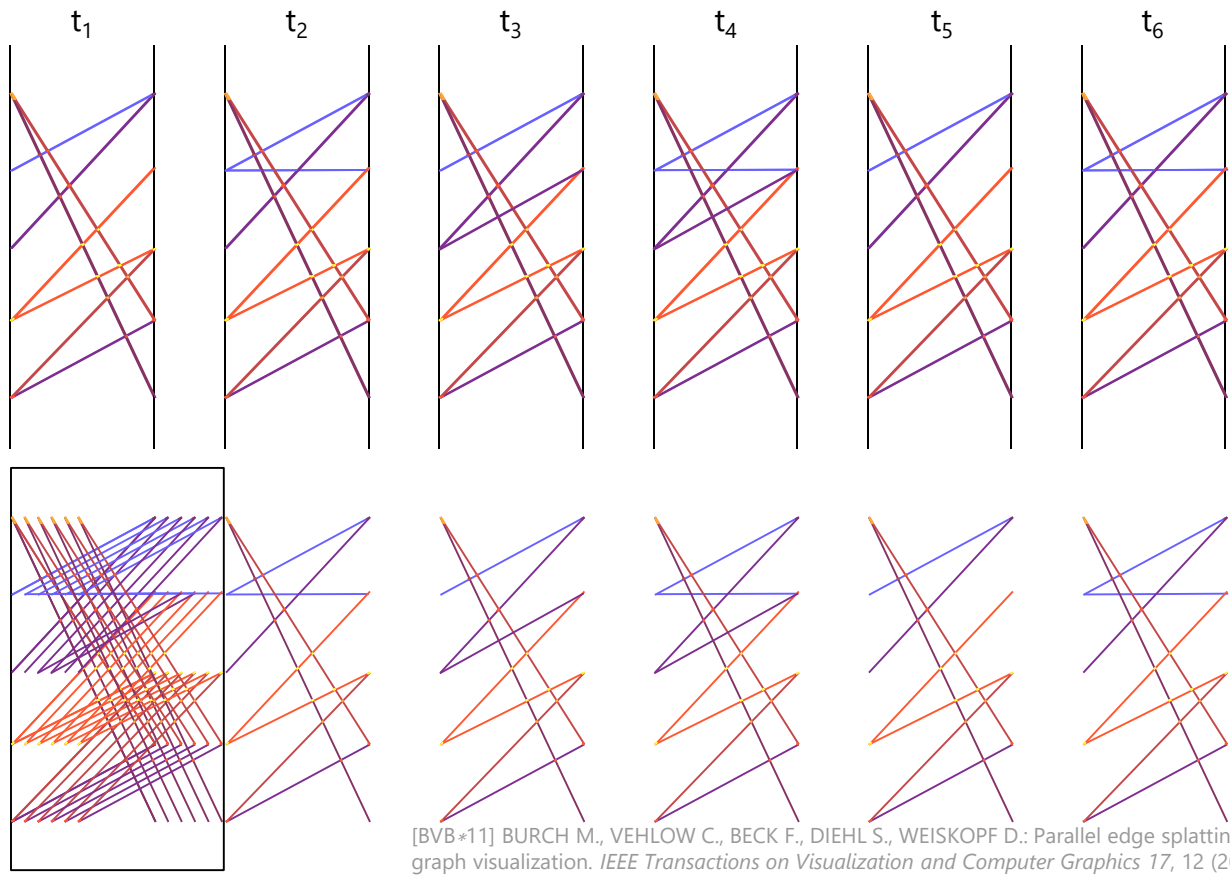


(d) Ordered bipartite graph layout



(e) Parallel edge splatting [BVB\*11]

\* Vertices are hierarchically clustered and then reordered by computing Jaccard similarities

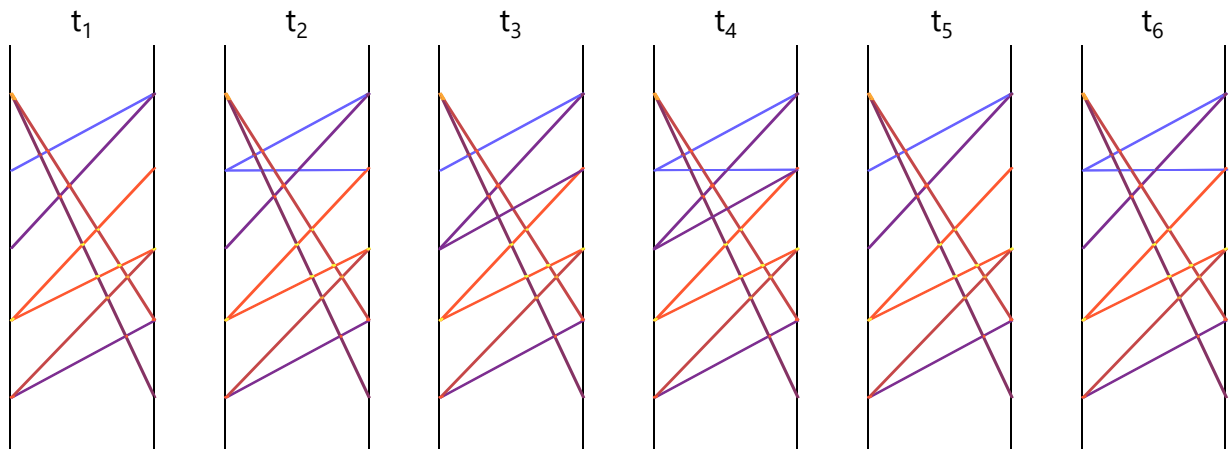


(e) Parallel edge splatting [BVB\*11]

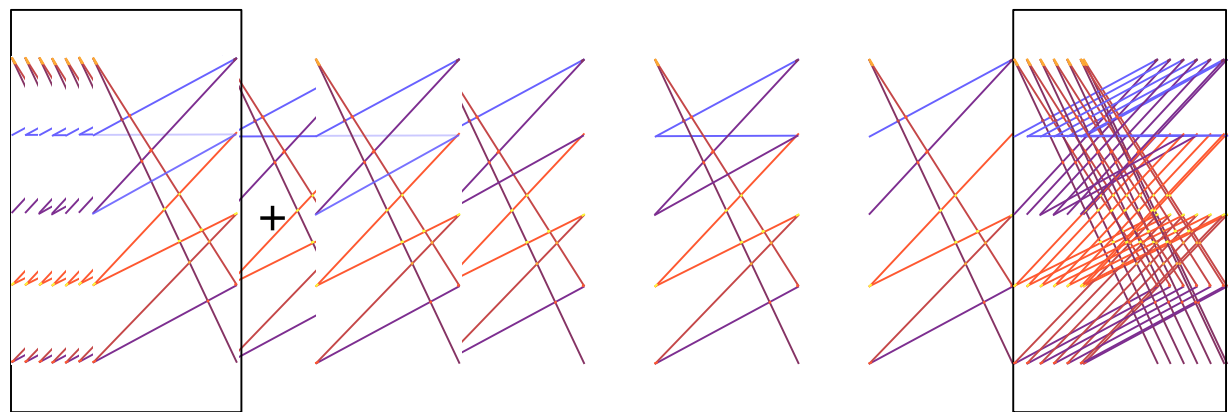
(f) Interleaving method [BHW17]

[BVB\*11] BURCH M., VEHLow C., BECK F., DIEHL S., WEISKOPF D.: Parallel edge splatting for scalable dynamic graph visualization. *IEEE Transactions on Visualization and Computer Graphics* 17, 12 (2011), 2344–2353. 2, 3

[BHW17] BURCH M., HLAwATSCH M., WEISKOPF D.: Visualizing a sequence of a thousand graphs (or even more). *Computer Graphics Forum* 36, 3 (2017), 261–271. 2, 3



(e) Parallel edge splatting [BVB\*11]

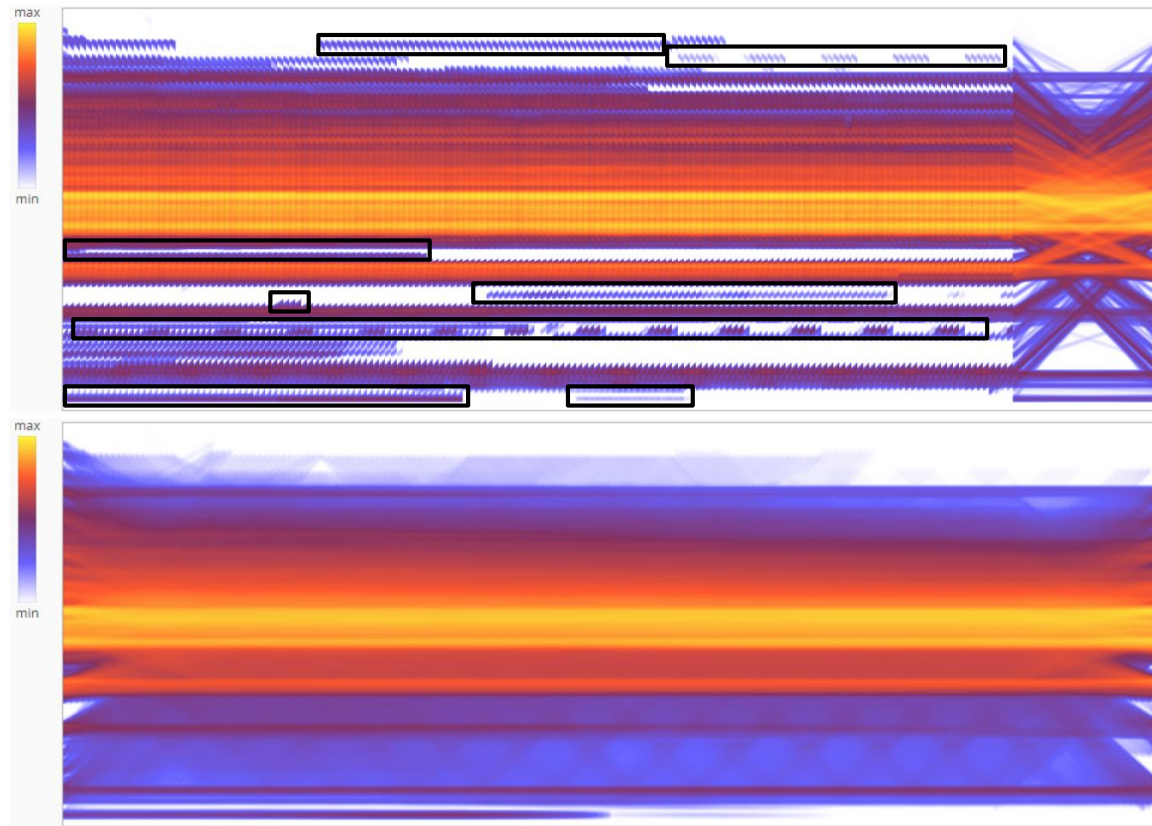


(f) Interleaving method [BHW17]

stacking

representative graph

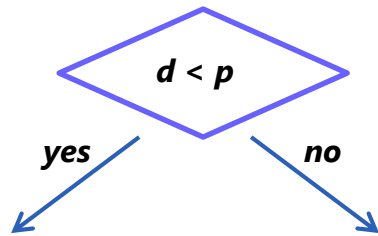




First 159 timepoints of the flight dataset visualized using stacked edge splatting (top) and the interleaving method (bottom). Temporal patterns are more recognizable in the top visualization

# Temporal Clustering

- Provides an overview of different temporal phases
- Improves the edge-tracing task
- Clustering is done sequentially by computing the Euclidian distance



*$t_i$  is added to the cluster  $c_j$     a new cluster creates for  $t_i$*

**$d$** : euclidian distance between  **$m(t_i)$**  and  **$m(c_j)$**

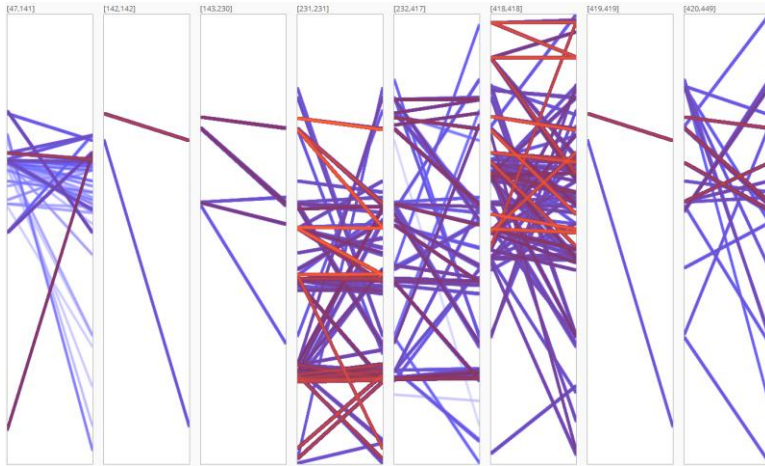
**$m(t_i)$** : adjacency matrix for the current timepoint  $t_i$

**$m(c_j)$** : adjacency matrix for the aggregated timepoint of the current cluster  $c_j$

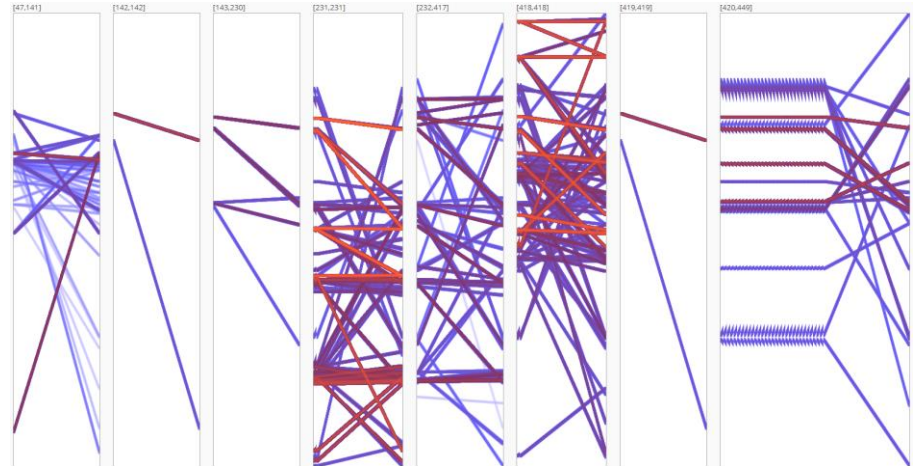
**$p$** : given threshold

# Temporal Clustering

- *collapsed view -> structural overview*
- *expanded view -> temporal details*



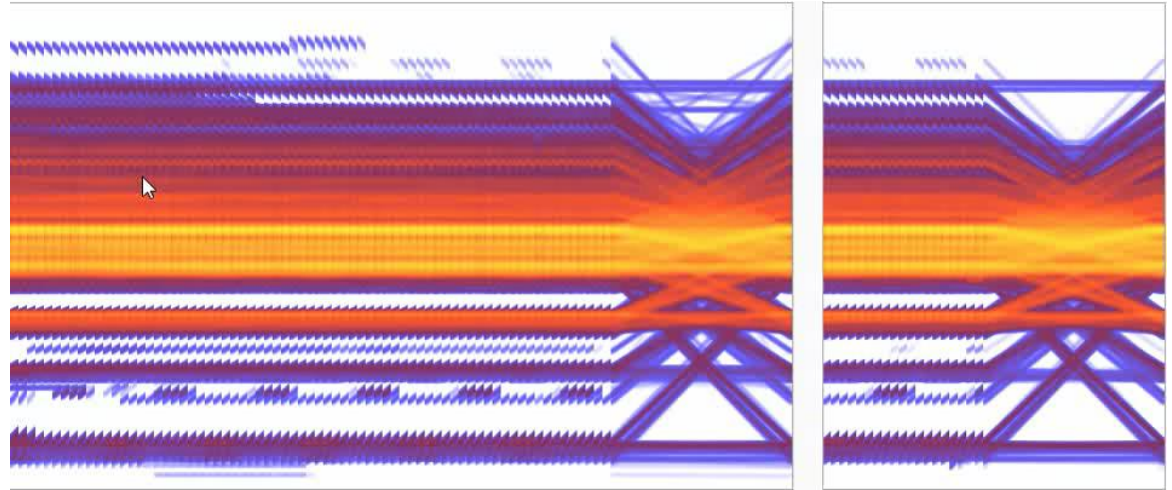
Default view, all clusters are collapsed



The last cluster is expanded

# When graphs are very dense

- Timepoint-expanding
- Edge-highlighting

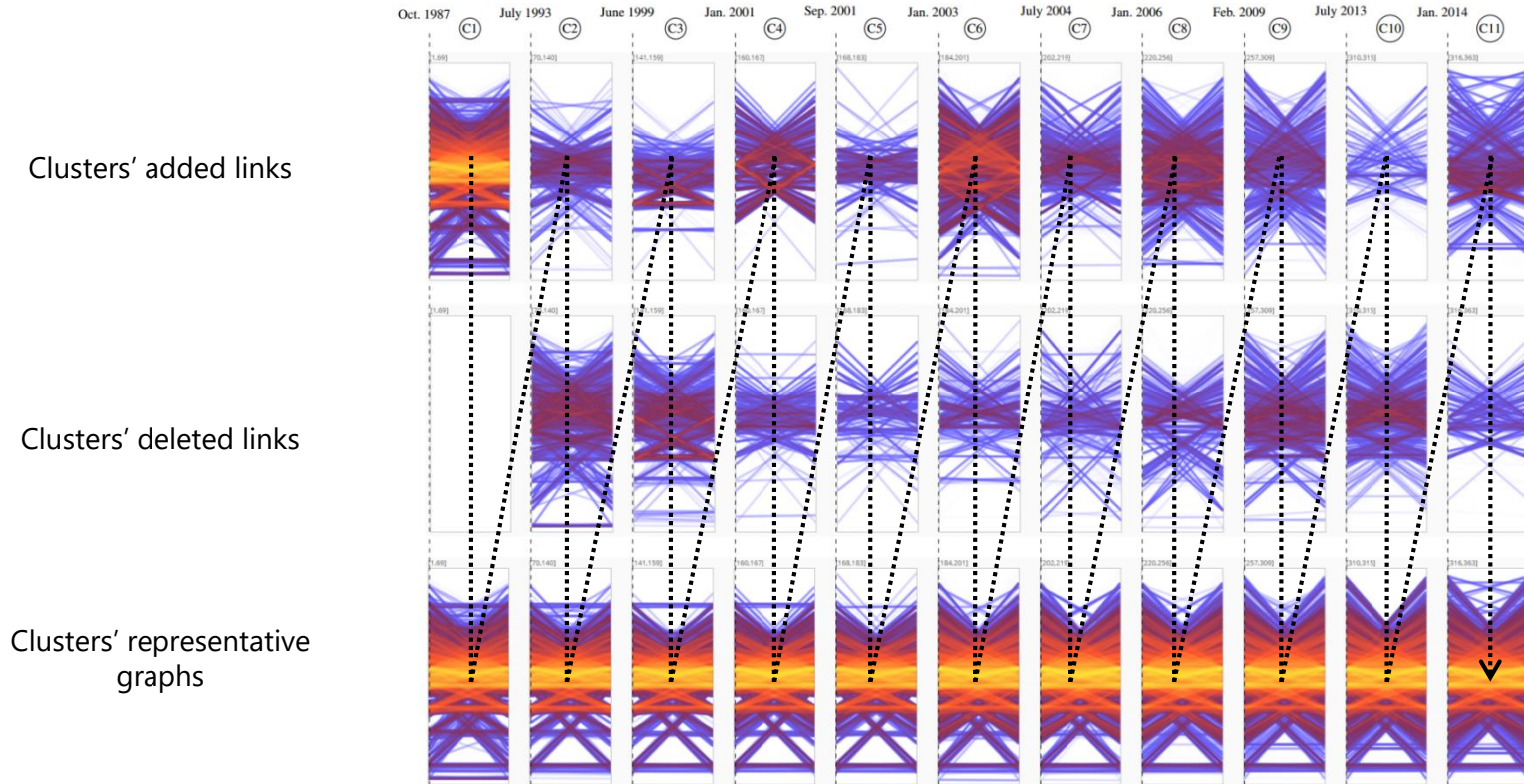


Interaction techniques

# Application Example

- US domestic flight traffic dataset [Uni18]
- 30 years starting from October 1st, 1987, to December 31st, 2017
- The data is aggregated on a per-month basis
- 402 vertices (airports)
- ~1 million weighted edges (flight connections)
- 363 timepoints (graphs per month)

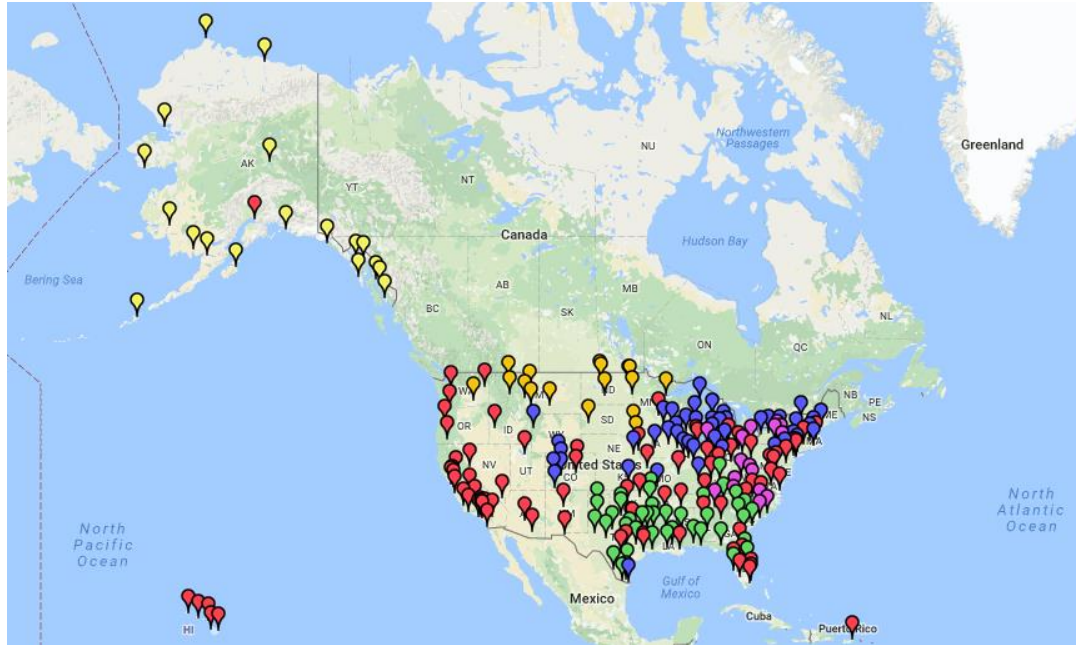
# Identifying temporal phases



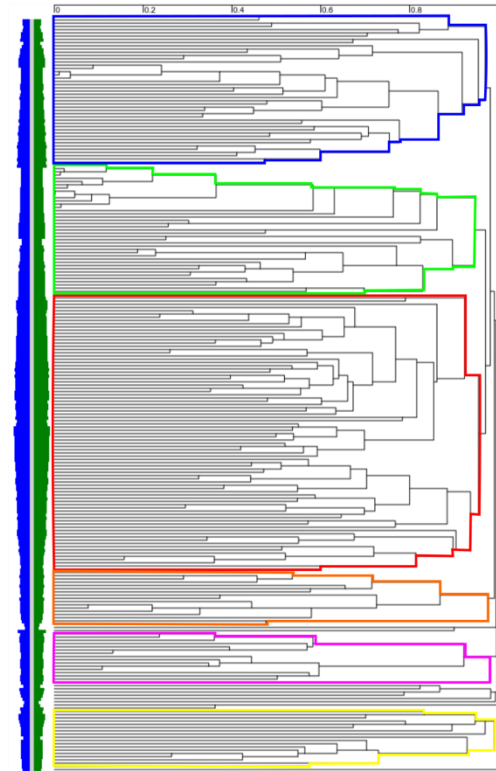
Sequentially clustering the flight dataset at a threshold of 1.1, resulting in 11 clusters



# Geographical Context

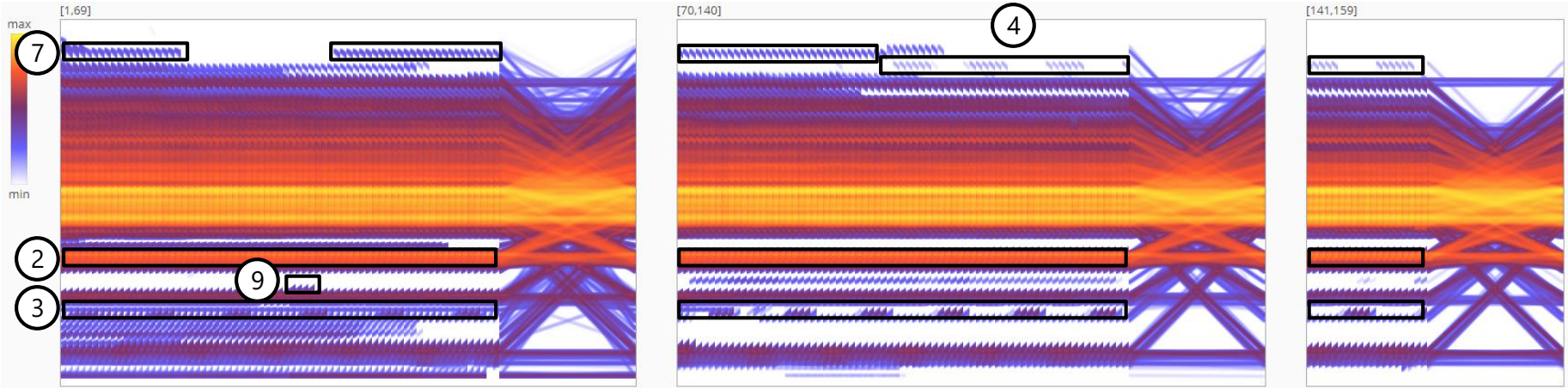


Vertex-clusters visualized on the map of the United States



Dendrogram of the vertex-clusters hierarchies

# Identifying temporal patterns



②  
Stability

③ ④  
Periodicity

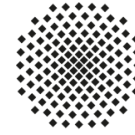
⑦  
Shift

⑨  
Anomalies



# Conclusion

- A time-scalable approach for visualizing dynamic graphs
- The stacking representation
  - To uncover temporal patterns
  - To achieve time-scalability
- Temporal clustering
  - To identify temporal phases
  - To improve the edge-tracing task
- For future work
  - Other heuristics for temporal clustering
  - Further evaluation



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Thanks 😊

Moataz Abdelaal  
VISUS, Universität Stuttgart  
[moataz.abdelaal@visus.uni-stuttgart.de](mailto:moataz.abdelaal@visus.uni-stuttgart.de)

# References

- [BVB\*11] BURCH M., VEHLow C., BECK F., DIEHL S., WEISKOPF D.: Parallel edge splatting for scalable dynamic graph visualization. *IEEE Transactions on Visualization and Computer Graphics* 17, 12 (2011), 2344–2353. 2, 3
- [BHW17] BURCH M., HLAwATSCH M., WEISKOPF D.: Visualizing a sequence of a thousand graphs (or even more). *Computer Graphics Forum* 36, 3 (2017), 261–271. 2, 3
- [vdEHBvW16] VAN DEN ELZEN S., HOLTEN D., BLAAS J., VAN WIJK J. J.: Reducing snapshots to points: A visual analytics approach to dynamic network exploration. *IEEE Transactions on Visualization and Computer Graphics* 22, 1 (2016), 1–10. 2
- [vdEHBvW13] VAN DEN ELZEN S., HOLTEN D., BLAAS J., VAN WIJK J. J.: Reordering massive sequence views: Enabling temporal and structural analysis of dynamic networks. In *Proceedings of IEEE Pacific Visualization Symposium* (2013), pp. 33–40. 2
- [GFC05] GHONIEM M., FEKETE J., CASTAGLIOLA P.: On the readability of graphs using node-link and matrix-based representations: a controlled experiment and statistical analysis. *Information Visualization* 4, 2 (2005), 114–135. 2
- [BHRD\*15] BACH B., HENRY-RICHE N., DWYER T., MADHYASTHA T., FEKETE J.-D., GRABOWSKI T.: Small MultiPiles: piling time to explore temporal patterns in dynamic networks. *Computer Graphics Forum* 34, 3 (2015), 31–40. 4

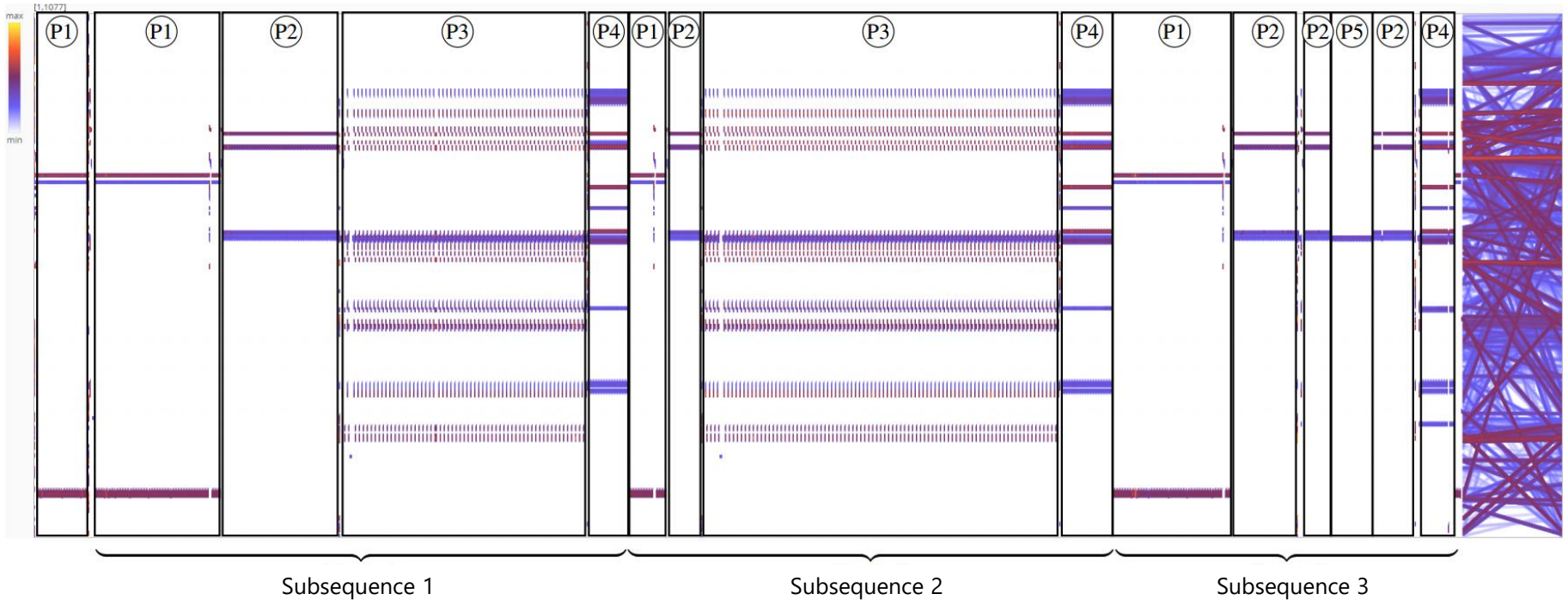
# References

- [BPF14] BACH B., PIETRIGA E., FEKETE J.: Visualizing dynamic networks with matrix cubes. In *Proceedings of Conference on Human Factors in Computing Systems* (2014), pp. 877–886. 2
- [Uni18] UNITED STATES DEPARTMENT OF TRANSPORTATION: OnTime Performance. [https://www.transtats.bts.gov/DL\\_SelectFields.asp?Table\\_ID=236&DB\\_Short\\_Name=On-Time](https://www.transtats.bts.gov/DL_SelectFields.asp?Table_ID=236&DB_Short_Name=On-Time), 2018. (Accessed on 03/22/2018). 2, 4
- [JHo18] JHotDraw Start Page. <http://www.jhotdraw.org/>, 2018. (Accessed on 03/22/2018). 2, 4

# Application Example (2)

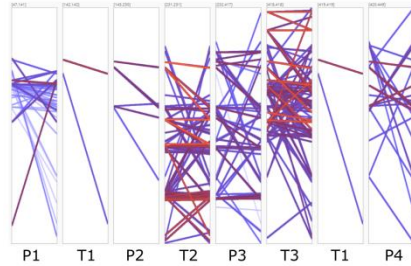
- The software call graph dataset [JHo18]
- 787 vertices (software functions)
- 25,906 weighted edges (call relations)
- 1,077 timepoints

# Identifying temporal patterns



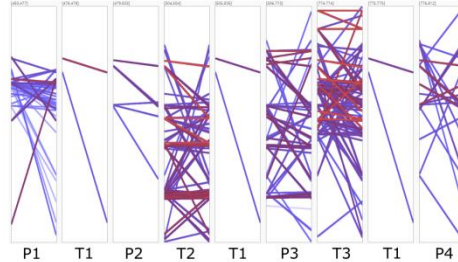
# Investigating subsequences

Subsequence 1 [47 – 449]



P: pattern (cluster)  
T: transition (single timepoint)

Subsequence 2 [450 – 812]



Subsequence 3 [813 – 1071]

